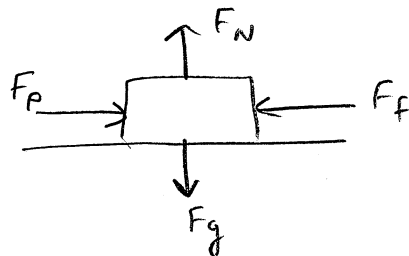


37

(a) $F_f = \mu F_N$



$$\mu = \frac{F_f}{F_N}$$

$$= \frac{F_p}{mg}$$

$$F_f = F_p$$

$$F_N = F_g = mg$$

$$= \frac{48.0 \text{ N}}{(5.0 \text{ kg})(9.81 \text{ m/s}^2)} = \underline{0.98}$$

(b) $F_{\text{net}} = ma$

$$F_p - F_f = ma$$

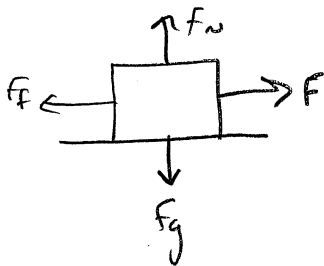
$$F_f = F_p - ma = 48 \text{ N} - (5 \text{ kg})(0.7 \text{ m/s}^2)$$

$$F_f = 44.5 \text{ N}$$

$$F_f = \mu F_N$$

$$\mu = \frac{F_f}{F_N} = \frac{F_f}{mg} = \frac{44.5 \text{ N}}{(5 \text{ kg})(9.81 \text{ m/s}^2)} = \underline{0.91}$$

39



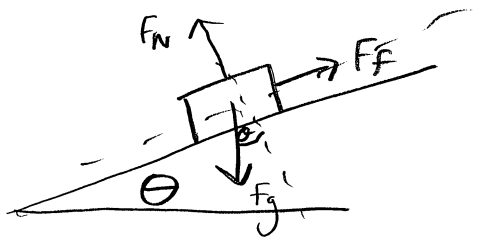
$$F_f = \mu F_N = \mu mg$$

$$F_f = F = ma$$

$$\mu mg = ma$$

$$a = (0.8)(9.81 \text{ m/s}^2) = \underline{7.8 \text{ m/s}^2}$$

40



$$F_f - F_g \sin \theta = 0$$

$$F_N - F_g \cos \theta = 0$$

$$F_f = mg \sin \theta$$

$$F_N = mg \cos \theta$$

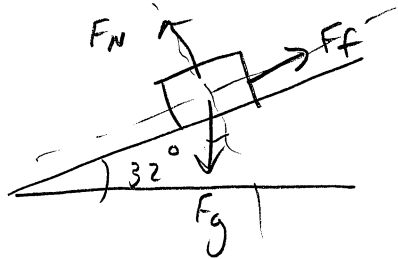
$$F_f = \mu F_N$$

$$mg \sin \theta = \mu mg \cos \theta$$

$$\theta = \tan^{-1}(\mu) = \tan^{-1}(0.8)$$

$$\theta = \underline{40^\circ}$$

41



$$-F_f + F_g \sin 32 = ma$$

$$F_f = mg \sin 32 - ma$$

$$= (15 \text{ kg})(9.81 \text{ ms}^{-2}) \sin 32 - (15 \text{ kg})(0.3 \text{ ms}^{-2})$$

$$= 73.48 \text{ N}$$

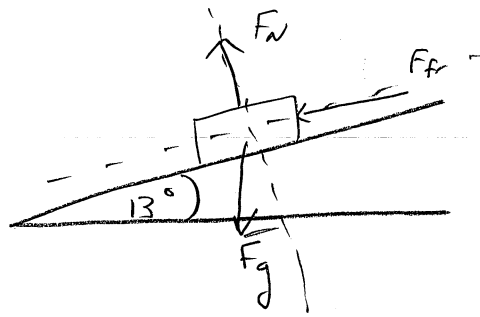
$$F_f = \underline{73 \text{ N}}$$

$$F_N = F_g \cos 32 = (15 \text{ kg})(9.81 \text{ ms}^{-2}) \cos 32 = 124.79 \text{ N}$$

$$F_f = \mu F_N$$

$$\mu = \frac{F_f}{F_N} = \frac{73.48 \text{ N}}{124.79 \text{ N}} = \underline{0.59}$$

(42)



$$F_f - F_g \sin \theta = ma$$

$$F_N = F_g \cos \theta$$

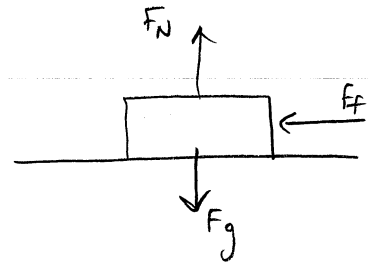
$$F_f = \mu F_N$$

$$a = \frac{\mu mg \cos \theta + mg \sin \theta}{m}$$

$$= (0.489)(9.81 \text{ ms}^{-2}) \cos 13 - (9.81 \text{ ms}^{-2}) \sin 13$$

$$a = 2.47 \text{ ms}^{-2}$$

The deceleration of the car is 2.47 ms⁻²



$$F_f = ma$$

$$F_N = F_g$$

$$F_f = \mu F_N$$

$$\mu = \frac{F_f}{F_N}$$

$$= \frac{ma}{mg}$$

$$= \frac{4.8 \text{ ms}^{-2}}{9.81 \text{ ms}^{-2}}$$

$$\mu = 0.489$$

(44)

$$s = 1000 \text{ m}$$

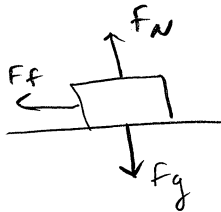
$$t = 12 \text{ s}$$

$$u = 0$$

$$a = ?$$

$$s = ut + \frac{1}{2}at^2$$

$$a = \frac{2s}{t^2} = \frac{2(1000 \text{ m})}{(12 \text{ s})^2} = 13.89 \text{ ms}^{-2}$$



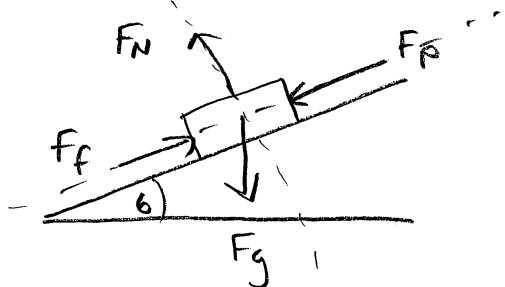
$$F_f = ma$$

$$F_N = F_g = mg$$

$$F_f = \mu F_N$$

$$\mu = \frac{F_f}{F_N} = \frac{ma}{mg} = \frac{13.89 \text{ ms}^{-2}}{9.81 \text{ ms}^{-2}} = 1.4$$

45



$$F_p - F_f + F_g \sin \theta = ma$$

$$F_N = F_g \cos \theta$$

$$F_f = \mu F_N$$

$$F_p = ma + \mu mg \cos \theta - mg \sin \theta$$

$$= 22 \text{ kg} (1.85 \text{ ms}^{-2} + 0.1 (9.81 \text{ ms}^{-2}) \cos 6 - (9.81 \text{ ms}^{-2}) \sin 6)$$

$$\underline{F_p = 40 \text{ N}}$$

$$u = 0$$

$$v = 60 \text{ kmh}^{-1} = 16.67 \text{ ms}^{-1}$$

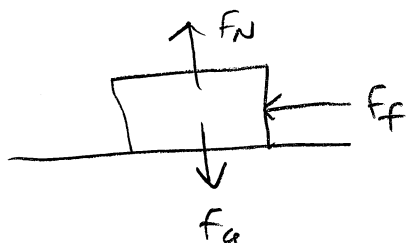
$$s = 75 \text{ m}$$

$$a = ?$$

$$v^2 = u^2 + 2as$$

$$a = \frac{v^2}{2s} = \frac{(16.67 \text{ ms}^{-1})^2}{2(75 \text{ m})} = 1.85 \text{ ms}^{-2}$$

47



$$F_f = ma$$

$$F_f = \mu F_N$$

$$F_N = F_g$$

$$\mu mg = ma$$

$$u = 4.0 \text{ ms}^{-1}$$

$$v = 0$$

$$a = \mu g$$

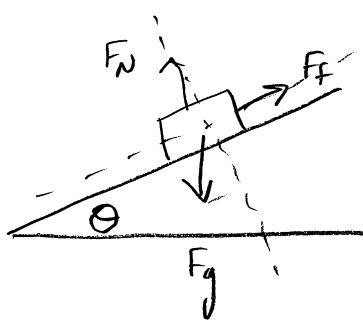
$$s = ?$$

$$v^2 = u^2 + 2as$$

$$s = \frac{u^2}{2a} = \frac{u^2}{2\mu g} = \frac{(4.0 \text{ ms}^{-1})^2}{2(.2)(9.81 \text{ ms}^{-2})}$$

$$\underline{s = 4.1 \text{ m}}$$

50



$$F_f = F_g \sin \theta$$

$$F_N = F_g \cos \theta$$

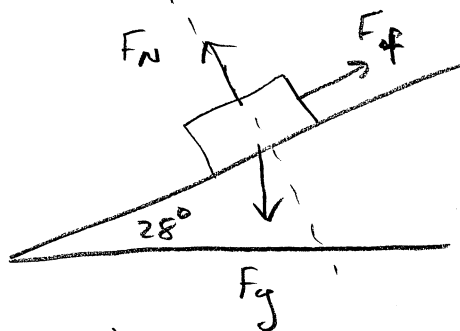
$$F_f = \mu F_N$$

$$F_g \sin \theta = \mu F_g \cos \theta$$

$$\theta = \tan^{-1}(\mu) = \tan^{-1}(.15) = 8.5^\circ$$

drive way will be safe if angle is $\leq 8.5^\circ$
 so only the 6° driveway is safe.

51



no friction

$$F_g \sin \theta = ma$$

$$a = g \sin \theta$$

$$u = 0$$

$$s = s$$

$$v = ?$$

$$v^2 = u^2 + 2as$$

$$v = \sqrt{2g \sin \theta s}$$

with friction

$$v = \frac{1}{2} \sqrt{2g \sin \theta s}$$

$$u = 0$$

$$s = s$$

$$a = ?$$

$$v^2 = u^2 + 2as$$

$$a = \frac{v^2}{2s} = \frac{\left(\frac{1}{2} \sqrt{2g \sin \theta s}\right)^2}{2s} = \frac{\frac{1}{4} 2g \sin \theta s}{2s}$$

$$a = \frac{g \sin \theta}{4}$$

continued next page

51 continued.

with friction

$$-F_f + F_g \sin \theta = ma$$

$$F_N = F_g \cos \theta$$

$$F_f = \mu F_N$$

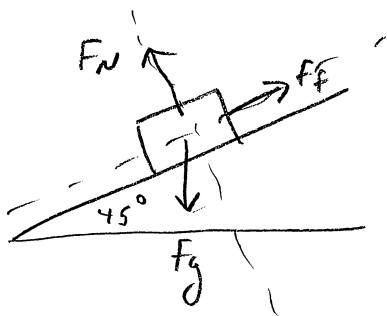
$$\mu = \frac{F_f}{F_N} = \frac{mg \sin \theta - ma}{mg \cos \theta}$$

$$= \frac{g \sin \theta - \frac{g \sin \theta}{4}}{g \cos \theta}$$

$$= \frac{3g \sin \theta}{4g \cos \theta}$$

$$= \frac{3 \tan \theta}{4} = \frac{3 \tan 28}{4} = \underline{0.40}$$

54



$$-F_f + F_g \sin \theta = ma$$

$$F_N = F_g \cos \theta$$

$$F_f = \mu F_N$$

$$a = -\mu g \cos \theta + g \sin \theta$$

$$= 9.81 \text{ m s}^{-2} (-.18 \cos 45 + \sin 45)$$

$$= 5.688 \text{ m s}^{-2}$$

$$u = 6.0 \text{ km h}^{-1} = 1.67 \text{ m s}^{-1}$$

$$a = 5.688 \text{ m s}^{-2}$$

$$s = 45.0 \text{ m}$$

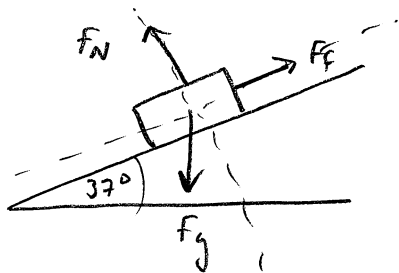
$$v = ?$$

$$v^2 = u^2 + 2as$$

$$v = \sqrt{(1.67 \text{ m s}^{-1})^2 + 2(5.688 \text{ m s}^{-2})(45 \text{ m})}$$

$$\underline{v = 23 \text{ m s}^{-1}}$$

55



$$-F_f + F_g \sin \theta = ma$$

$$F_f = mg \sin \theta - ma$$

$$= (18 \text{ kg})(9.81 \text{ ms}^{-2}) \sin 37 - (18 \text{ kg})(0.27 \text{ ms}^{-2})$$

$$= 101.4 \text{ N}$$

$$\underline{F_f = 101 \text{ N}}$$

$$F_f = \mu F_N$$

$$F_N = F_g \cos \theta$$

$$\mu = \frac{F_f}{F_N} = \frac{F_f}{mg \cos \theta} = \frac{101.4 \text{ N}}{(18 \text{ kg})(9.81 \text{ ms}^{-2}) \cos 37}$$

$$\underline{\mu = 0.95}$$

58

(a) $F_f = ma$

$$F_f = \mu F_N = \mu mg$$

$$ma = \mu mg$$

$$u = v$$

$$v = 0$$

$$a = -\mu g$$

$$s = ?$$

$$v^2 = u^2 + 2as$$

$$s = \frac{-u^2}{2a} = \frac{-v^2}{2(-\mu g)} = \frac{v^2}{2\mu g}$$

(continued next page)

$$58 \text{ (b)} \quad u = 95 \text{ km h}^{-1} = 26.39 \text{ ms}^{-1}$$

$$m = 1200 \text{ kg}$$

$$\mu = 0.75$$

$$s = \frac{v^2}{2\mu g} = \frac{(26.39 \text{ ms}^{-1})^2}{2(0.75)(9.81 \text{ ms}^{-2})} = \underline{47 \text{ m}}$$

$$(70) \quad F_f = \mu F_N = \mu mg = ma$$

$$a = -\mu g$$

$$u = ?$$

$$s = 72 \text{ m}$$

$$v = 0$$

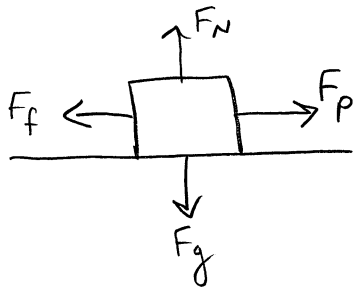
$$v^2 = u^2 + 2as$$

$$u = \sqrt{-2as}$$

$$= \sqrt{-2(-\mu g)s} = \sqrt{+2(+.8)(9.81 \text{ ms}^{-2})72 \text{ m}}$$

$$\underline{u = 34 \text{ ms}^{-1}}$$

76 (a)



max F_p occurs when $F_p = F_f = \mu F_N$

$$F_p = \mu m_{\text{block}} g$$

but F_p is a result of sand in the bucket



$$F_p = F_g = (m_{\text{bucket}} + m_{\text{sand}}) g$$

$$\therefore (m_{\text{bucket}} + m_{\text{sand}}) g = \mu m_{\text{block}} g$$

$$m_{\text{sand}} = \mu m_{\text{block}} - m_{\text{bucket}}$$
$$= (0.45)(28 \text{ kg}) - 1.35 \text{ kg}$$

$$\underline{m_{\text{sand}} = 11.25 \text{ kg}}$$

$$(b) F_p - F_f = ma$$

$$(m_{\text{bucket}} + m_{\text{sand}}) g - \mu m_{\text{block}} g = (m_{\text{block}} + m_{\text{bucket}} + m_{\text{sand}}) a$$

$$a = \frac{(m_{\text{bucket}} + m_{\text{sand}}) g - \mu m_{\text{block}} g}{(m_{\text{block}} + m_{\text{bucket}} + m_{\text{sand}})}$$

$$= \frac{(1.35 \text{ kg} + 11.25 \text{ kg})(9.81 \text{ ms}^{-2}) - (0.32)(28 \text{ kg})(9.81 \text{ ms}^{-2})}{(28 \text{ kg} + 1.35 \text{ kg} + 11.25 \text{ kg})}$$

$$\underline{a = 0.880 \text{ ms}^{-2}}$$

$$\textcircled{83} \quad F_f = ma = \mu F_N = \mu mg$$

$$a = -\mu g$$

$$v = 0$$

$$s = 75 \text{ m}$$

$$u = ?$$

$$v^2 = u^2 + 2as$$

$$u = \sqrt{-2as} = \sqrt{+2(+\mu g)s}$$

$$= \sqrt{2(.1)(9.81 \text{ ms}^{-2})(75 \text{ m})}$$

$$\underline{u = 12 \text{ ms}^{-1}}$$